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The system of deterministic equations describing the processes of microplastic pollution influence in shallow water on the growth rate and development of a commercial fish population has the form:

$$(P_i)'_t + \operatorname{div}(\mathbf{u}P_i) = \mu_i \Delta P_i + \varphi_i, i \in \overline{1, 7},$$

where  $P_i$  is the concentration of  $i$ -th component: 1, 2 are phytoplankton (*Chlorella vulgaris* Beijer green algae and its metabolite), 3 is the biogenic substance, 4 is the zooplankton, 5 is the commercial fish (*Abramis brama* bream), 6, 7 are micro- and nanoplastics;  $\mathbf{u}$  is the vector of water flow velocity;  $\mu_i$  are diffusion coefficients;  $\varphi_i$  is a chemical and biological source [1].

**The theorem.** Let the equation of the considered system at  $i = 5$  taking into account the environment fluctuations have the form:  $\dot{P}_5 = (\alpha_5 - \beta_5 + y(t))P_5$ ,  $m(t) = P_5^0 \exp\{(\alpha_5 - \beta_5)t\}$ ,  $\sigma^2(t) = P_5^0 \exp\{2(\alpha_5 - \beta_5)t\}(\exp\{\sigma^2 t\} - 1)$ ,  $\alpha_5$ ,  $\beta_5$  are growth rate and mortality of commercial fish;  $\gamma = \alpha_5 - \beta_5$ ,  $P_5^0$  is the concentration of  $P_5$  at initial time;  $m(t)$ ,  $\sigma^2(t)$  are mathematical expectation and variance of fluctuations  $y(t)$ . Then, the probability of degeneration of *Abramis brama* increases over time at  $\gamma < \sigma^2$ , tending to unity in the limit – the population is probabilistically unstable, i.e. a sufficiently prolonged exposure to disturbances (penetration and ingestion of micro- and nanoplastics particles by fish) can most likely lead to its death. The probability of degeneration decreases at  $\gamma > \sigma^2$  and tends to zero at  $t \rightarrow \infty$  – the population is stable in this sense.

## СПИСОК ЛИТЕРАТУРЫ

- [1] A. Yu. Perevaryukha, “Models of population process with delay and the scenario for adaptive resistance to invasion”, *Computer Research and Modeling*, **14** (1) (2022), 147–161. DOI:10.20537/2076-7633-2022-14-1-147-161.

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